

*Blazar Population Estimates*

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# History

1991: 1  $\gamma$ -ray blazar: 3C273

5 April 1991: Launch of GRO

1992:  $\gamma$ -ray blazar class: 3C 279, 3C 273,  
PKS 0528+134...

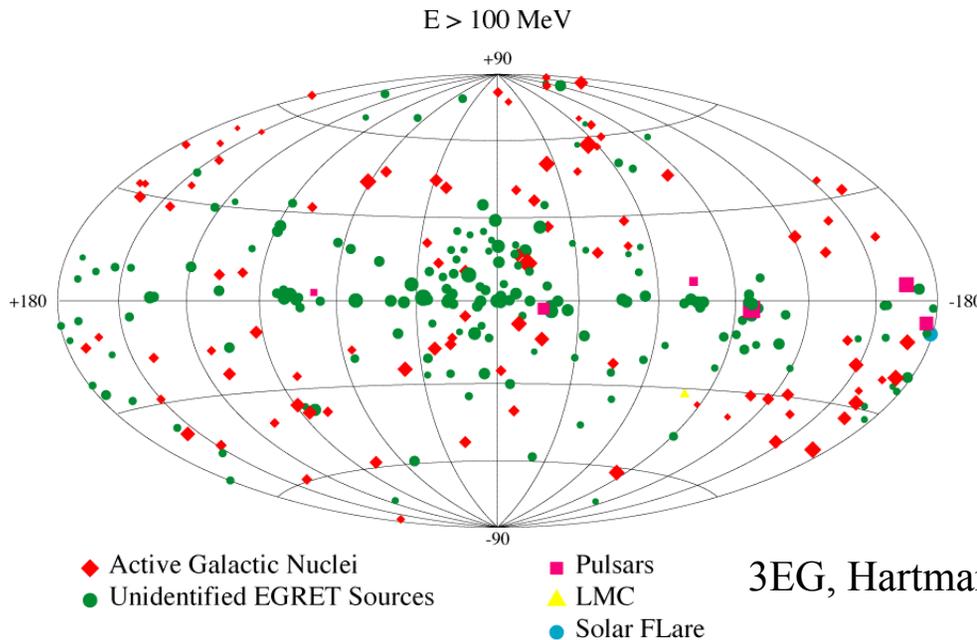
1995: 40/51 EGRET blazars

2EG, Thompson et al. (1995)

von Montigny et al. (1995)

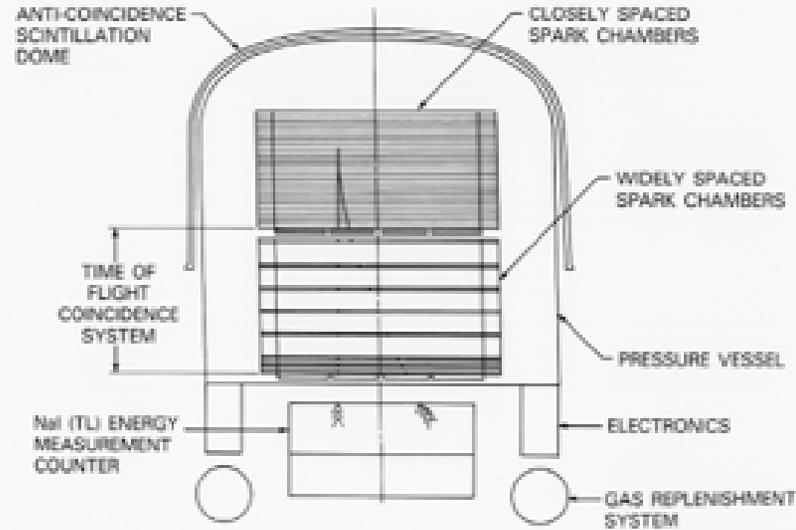
Mukherjee et al. (1997)

Third EGRET Catalog



3EG, Hartman et al. (1999)

# The EGRET



**Relativistically beamed emission:**

**superluminal sources**

**radio connection**

**Flat Spectrum radio sources**

**Kuehr catalog**

**blazars (incl. LBLs and HBLs)**

**Blue blazar/TeV connection**

# $\gamma$ -ray Population Studies

Stecker and Salamon (1996)

assuming radio- $\gamma$  correlation

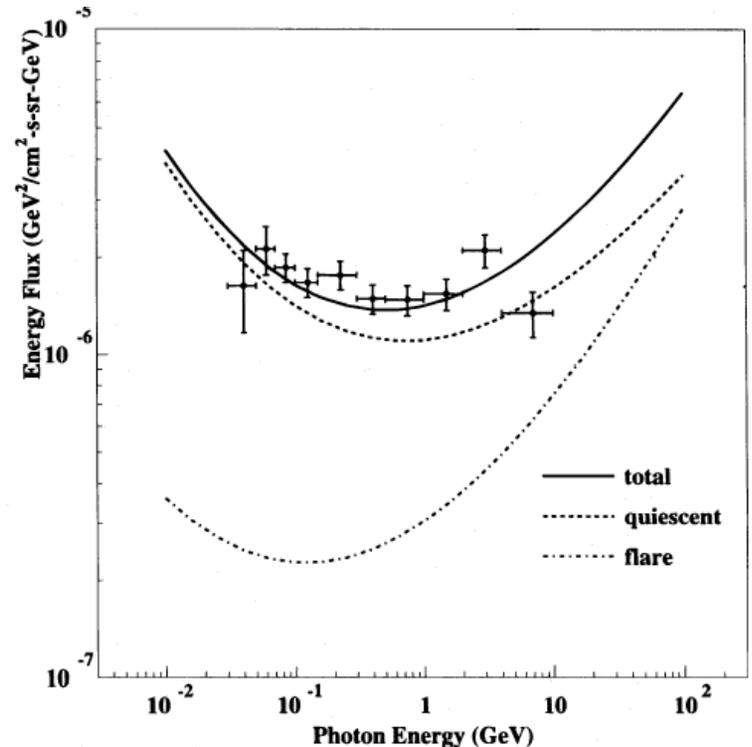
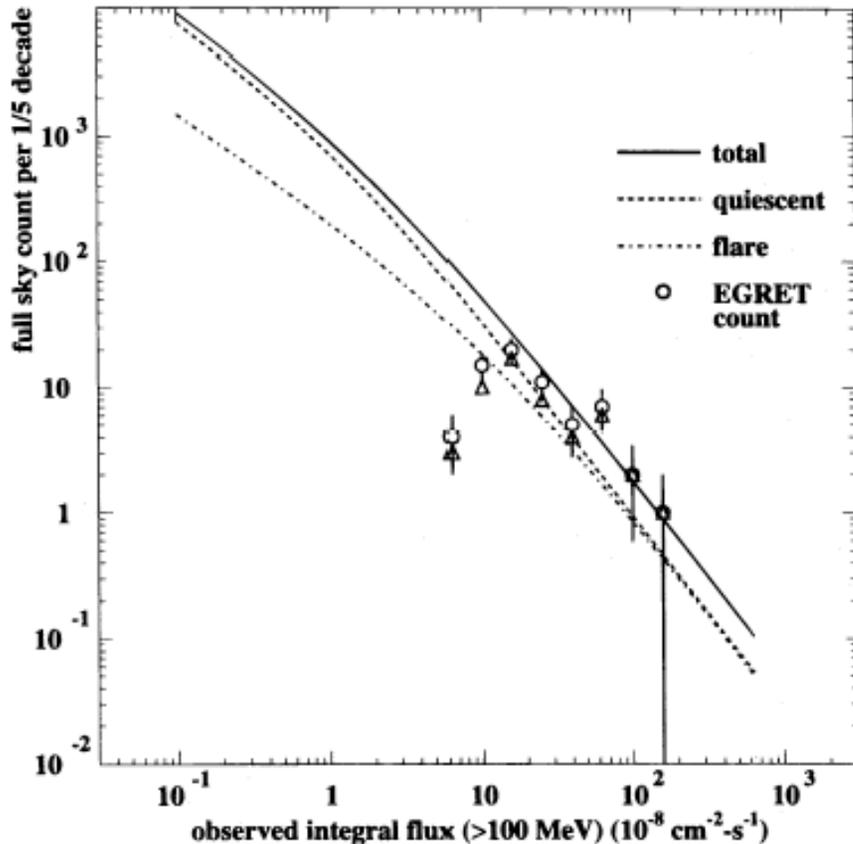
(see also talk by Paolo Giommi)

RLF

$$\rho_r(P_r, z) = 10^{-8.15} \left\{ \left[ \frac{P_r}{P_c(z)} \right]^{0.83} + \left[ \frac{P_r}{P_c(z)} \right]^{1.96} \right\}^{-1}$$

$\gamma$ LF

$$\rho_\gamma(P_{\gamma f}, z) = (1 - \zeta)\eta\rho_r\left(\frac{P_{\gamma f}}{\kappa}, z\right) + \zeta\eta\rho_r\left(\frac{P_{\gamma f}}{A\kappa}, z\right)$$



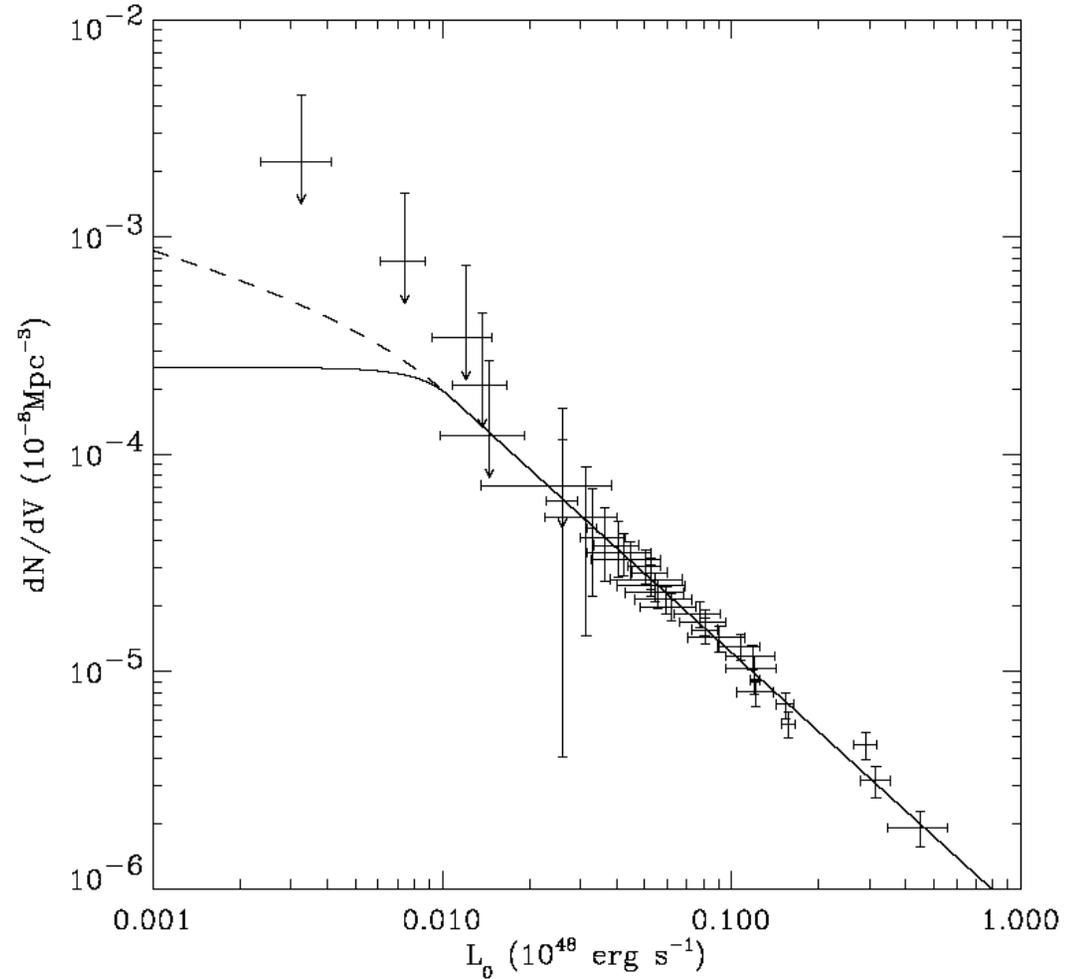
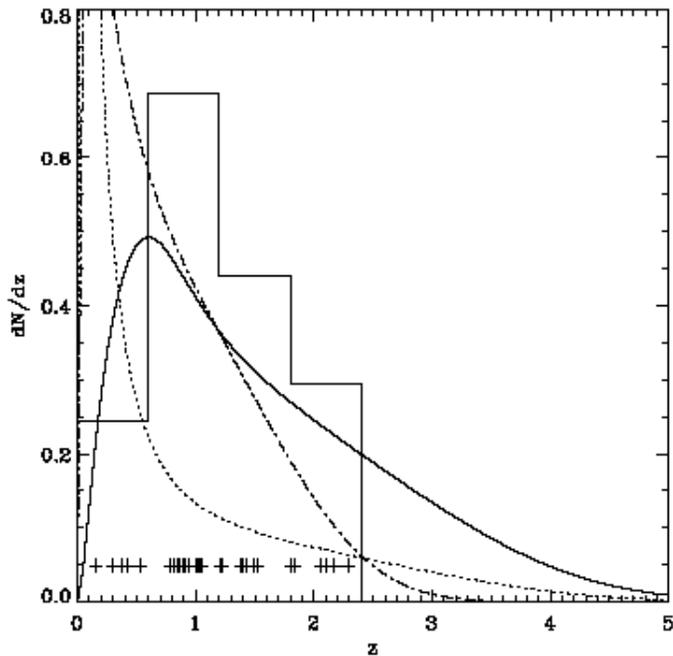
# $\gamma$ -ray Population Studies with Luminosity Evolution

Chiang et al. (1995)

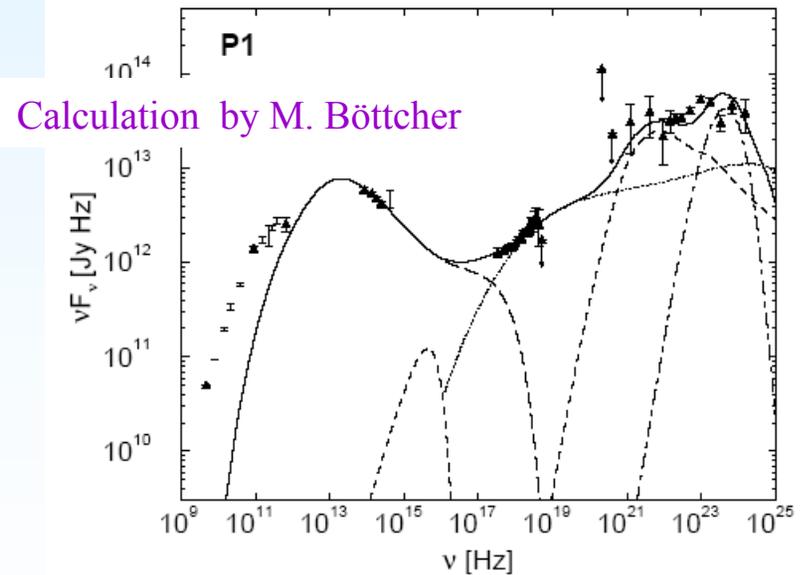
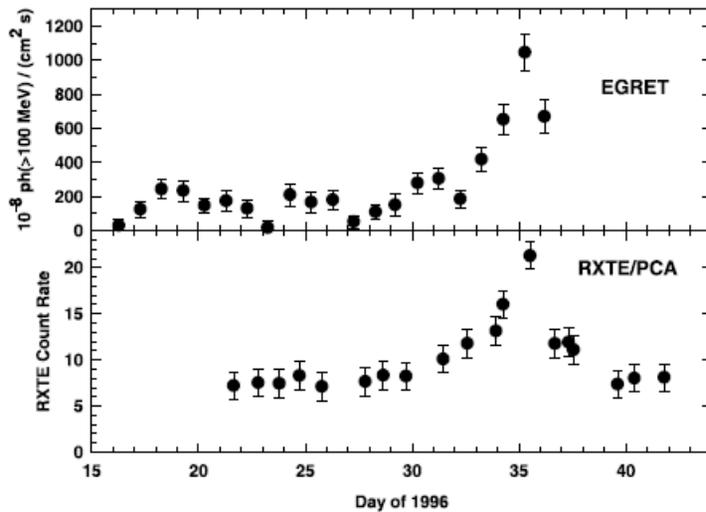
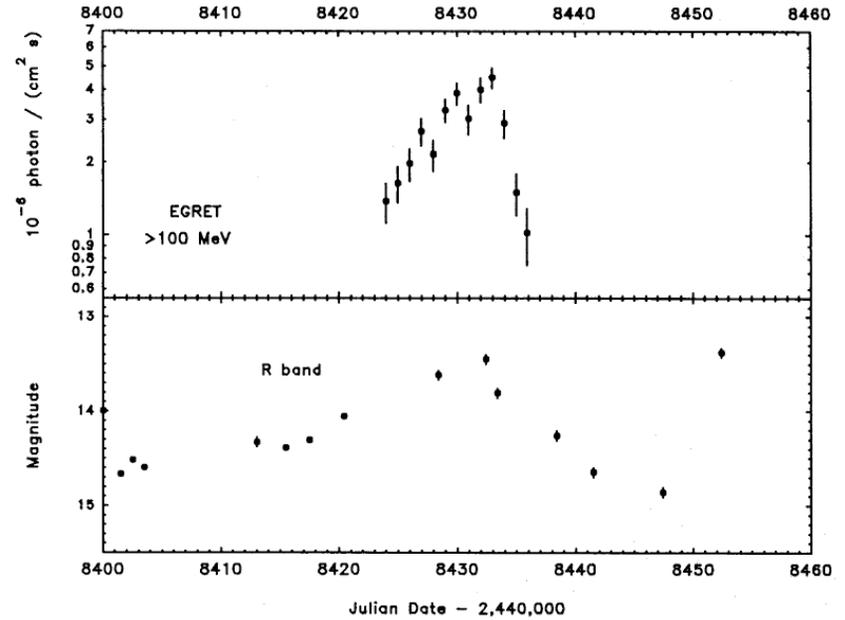
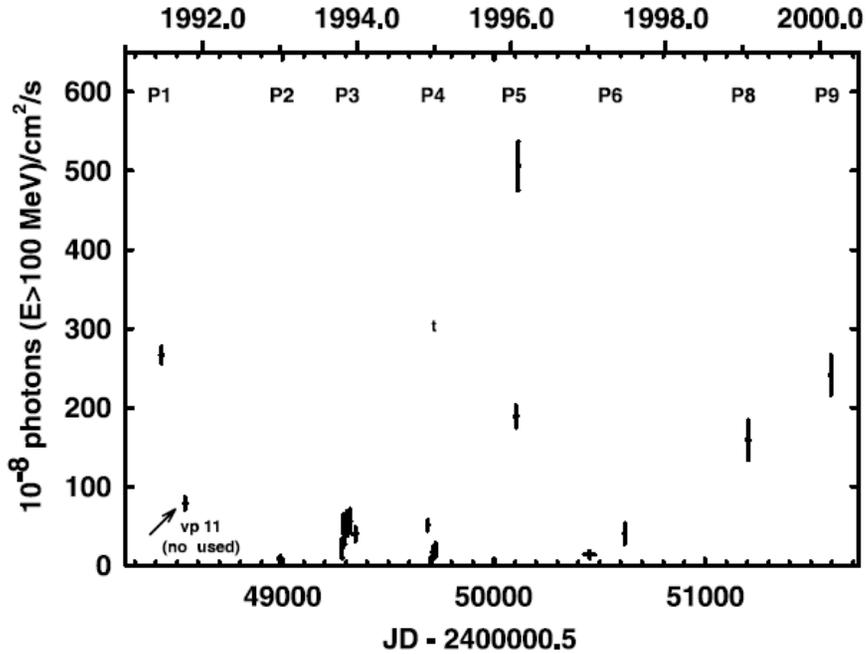
Chiang and Mukherjee (1997)

Narumoto and Totani (2005)

Giommi and Colafrancesco  
(2006)

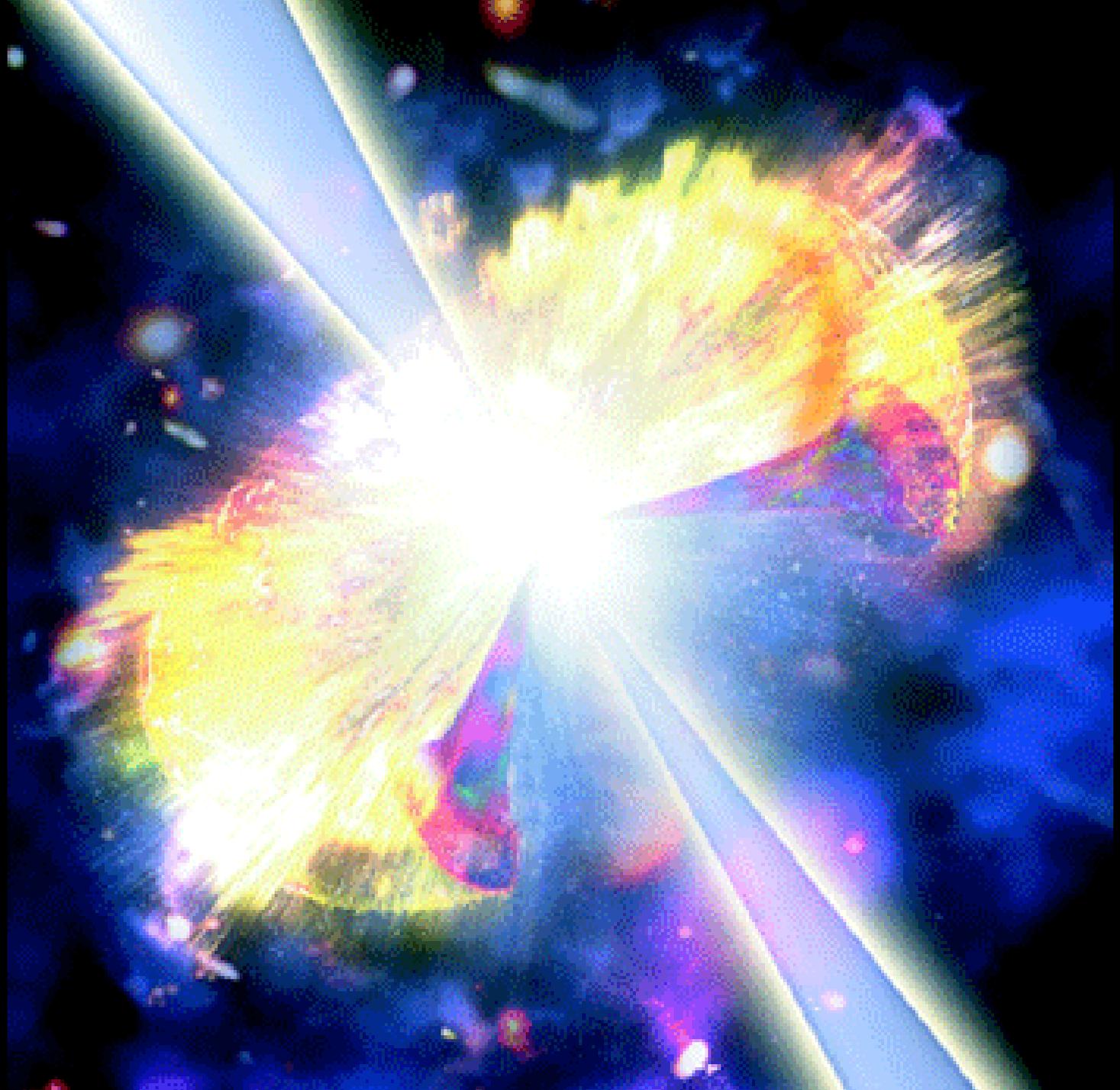


# 3C 279 Variability

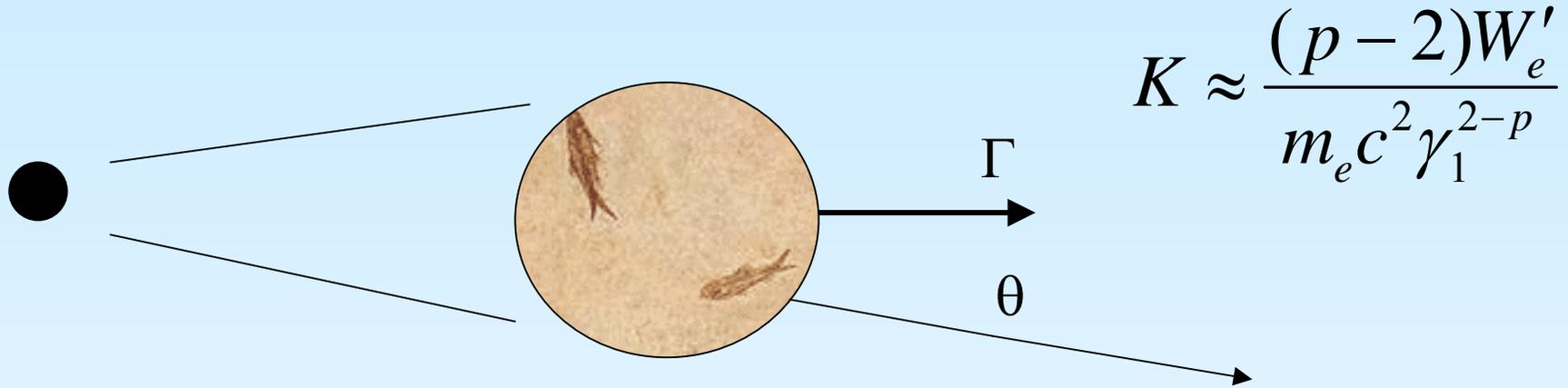


Calculation by M. Böttcher

Hartman et al. 1992, 1996, 2000



## Physical Model

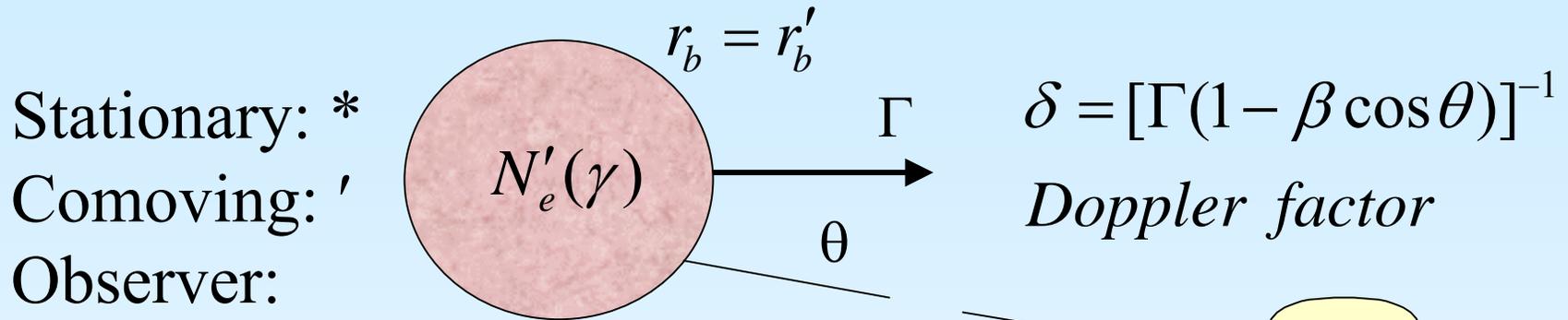


*Power-law electron distribution:*

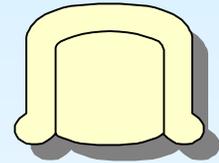
$$N'_e(\gamma) = K\gamma^{-p} H(\gamma; \gamma_1, \gamma_2); W'_e = \text{nonthermal electron energy}$$

$$f_{\varepsilon}^{proc} \cong \frac{\ell'_e}{d_L^2} \delta_D^q \varepsilon_z^{(3-p)/2}$$

# Nonthermal Radiation Physics of Jets: Synchrotron Emission



$$\nu F_\nu = f_\varepsilon = \delta^4 \frac{L'}{4\pi d_L^2}$$



$$\nu F_\nu = f_\varepsilon^{syn} = \frac{\delta^4}{d_L^2} \varepsilon' J(\varepsilon', \Omega') \cong \frac{\delta^4}{6\pi d_L^2} c \sigma_T u_B \gamma_s^3 N'_e(\gamma_s),$$

$$\gamma_s = \sqrt{\frac{(1+z)\varepsilon}{\delta(B/B_{cr})}}$$

$$u_B = B^2 / 8\pi$$

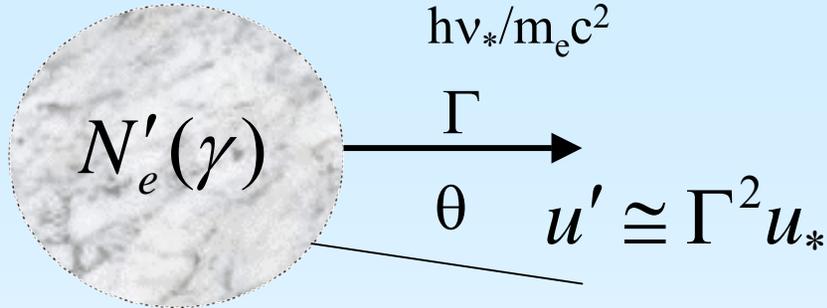
$$B_{cr} = m_e^2 c^3 / e\hbar$$

*Critical magnetic field*

$$\mathbf{q} = (\mathbf{p}+5)/2$$

# External Compton (EC)

target photon energy  $\varepsilon_* =$   
 $h\nu_*/m_e c^2$



$$FSRQ: u_* \sim \text{ergs cm}^{-3}$$

$$\varepsilon_* \cong 10^{-4} M_8^{-1/4}$$

$$q = p+3$$

$$CMBR: u_* = 4 \times 10^{-13} (1+z)^4 \text{ ergs cm}^{-3}, \varepsilon_* \cong 1.3 \times 10^{-9} (1+z)$$



$$\nu F_\nu = f_\varepsilon^{EC} \cong \frac{\delta^6}{6\pi d_L^2} c \sigma_T u_* \gamma_{EC}^3 N'_e(\gamma_{EC})$$

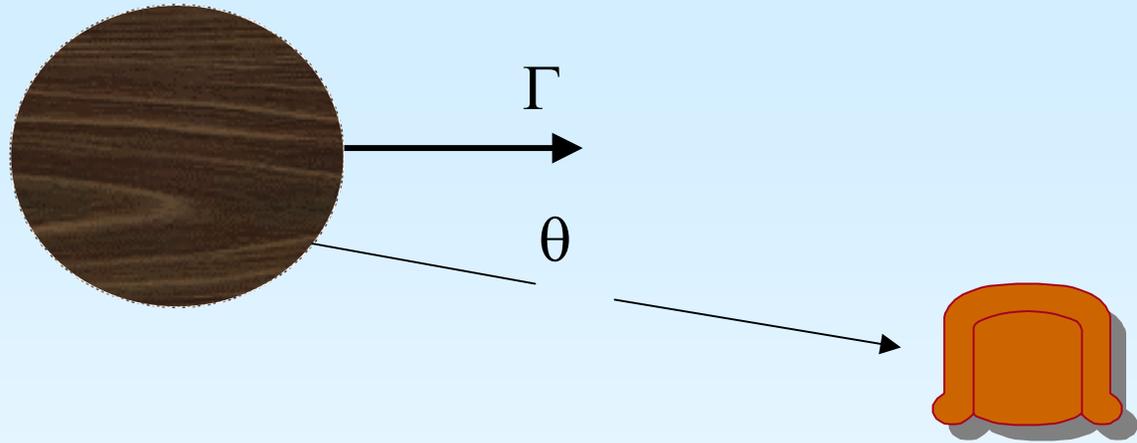
$$\gamma_{EC} = \frac{1}{\delta} \sqrt{\frac{(1+z)\varepsilon}{2\varepsilon_*}}$$

$$f_{\varepsilon_s}^{EC} / f_{\varepsilon_{EC}}^{syn} \propto \delta_D^{(p+1)/2} \propto \delta_D^{1+\alpha}$$

CD (1995), DSS (1997)

## Synchrotron self-Compton (SSC)

$$\frac{n'_{syn}(\epsilon')}{\dot{N}_{syn}(\epsilon')} \approx \frac{4\pi r_b^2 c}{4\pi r_b^2 c}$$

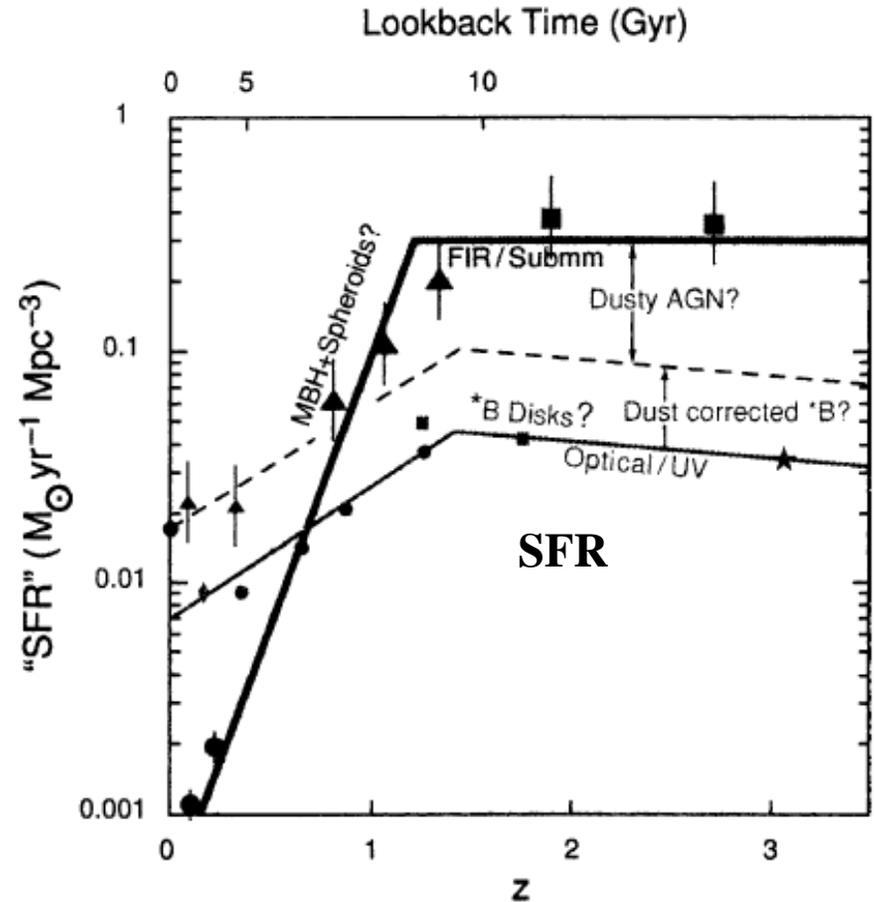
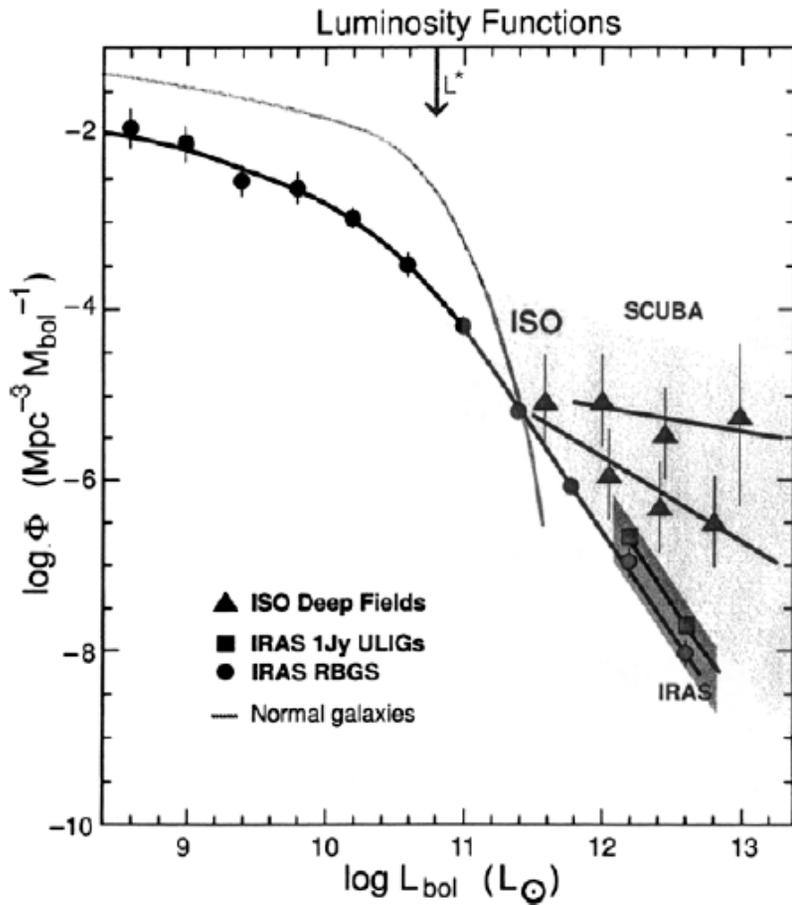


$$\nu F_\nu = f_\epsilon^{SSC} \cong \frac{\delta^4}{9\pi d_L^2} \frac{c \sigma_T^2 r_b u_B K^2}{V_b'} \gamma_s^{3-p} \Sigma_C$$

$$f_\epsilon^{SSC} \propto \delta^{(5+p)/2} B^{(9+p)/2} \epsilon_z^{(3-p)/2}$$

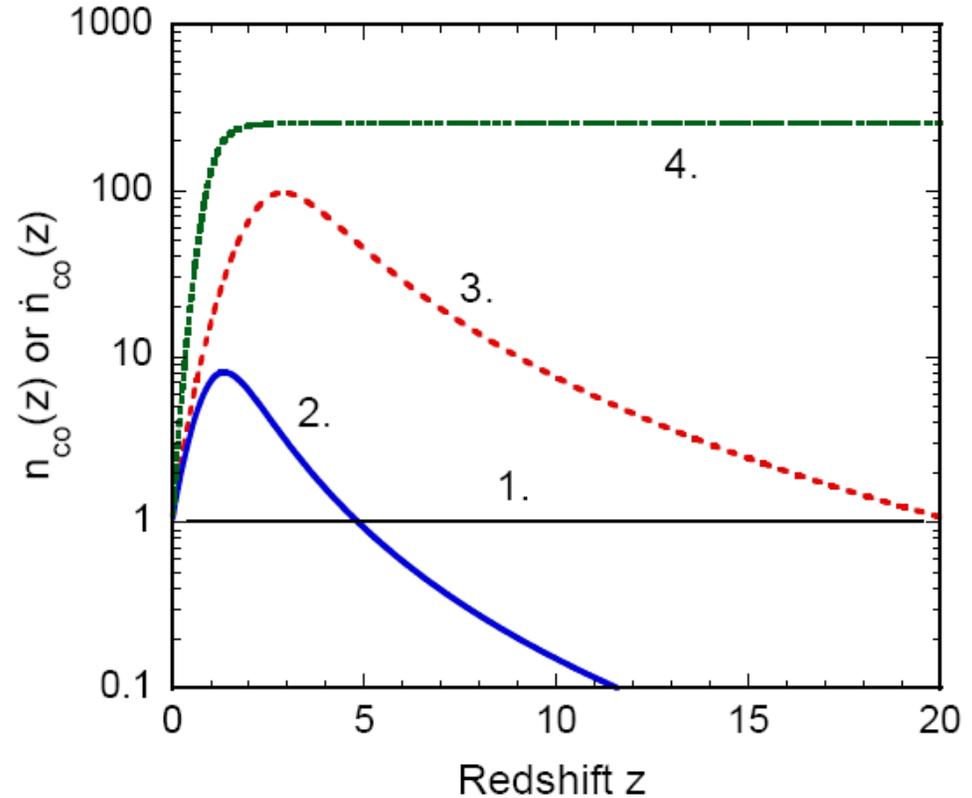
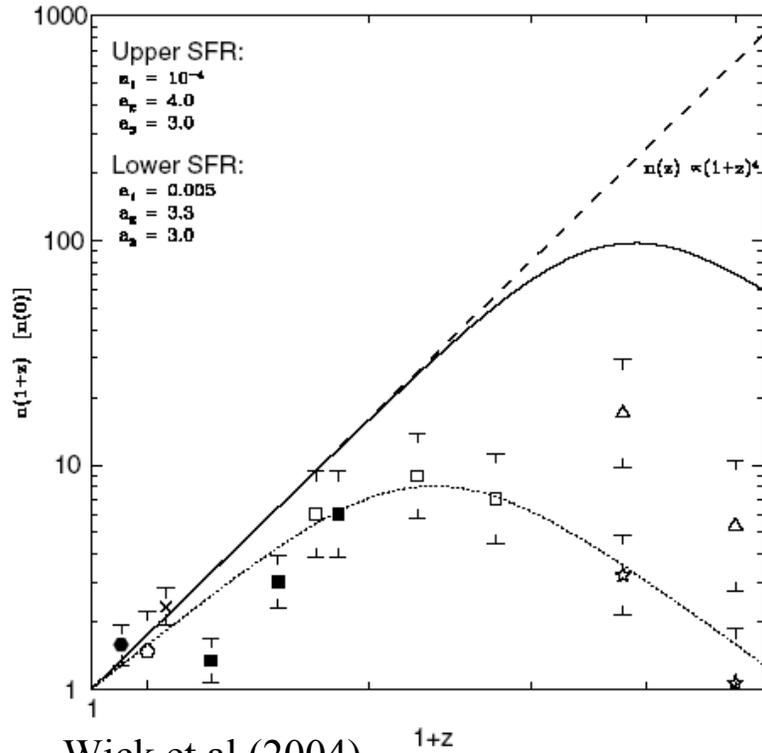
Same beaming factor as synchrotron

# Density and Luminosity Evolution of IR galaxies: 30 – 300 $\mu$ (900 GHz)



Sanders (2004)

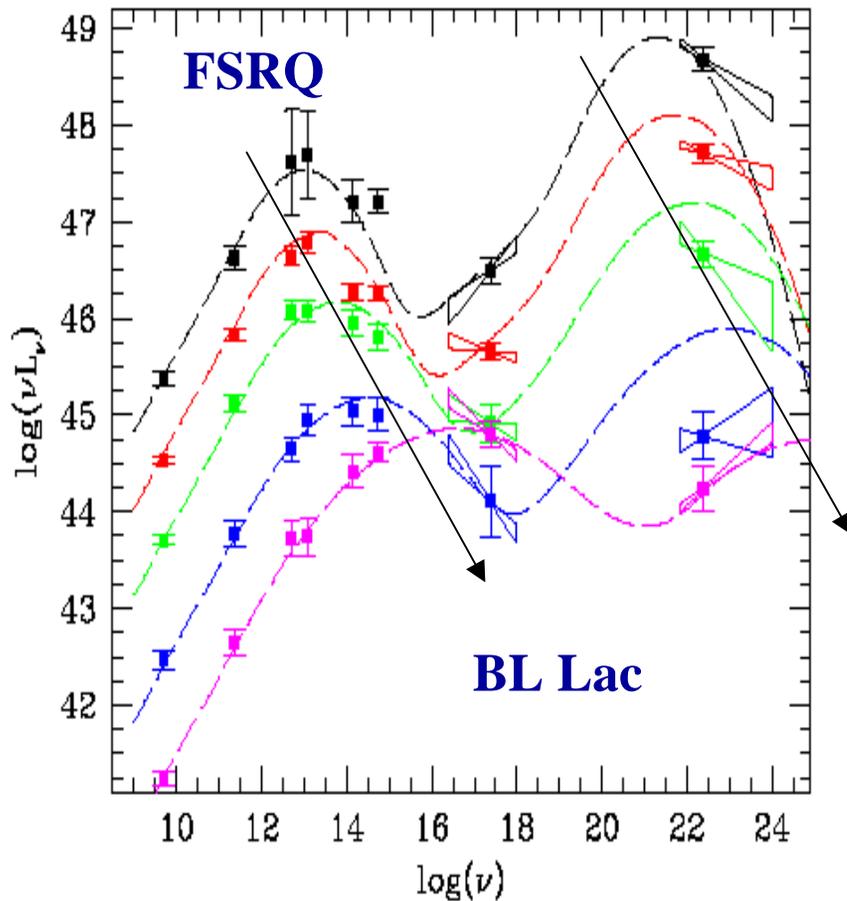
# Analytic Blazar Formation Rate



1. Constant Comoving Density
2. “Madau” curve
3. SFR with extinction corrections
4. Evolution of IR from IR galaxies

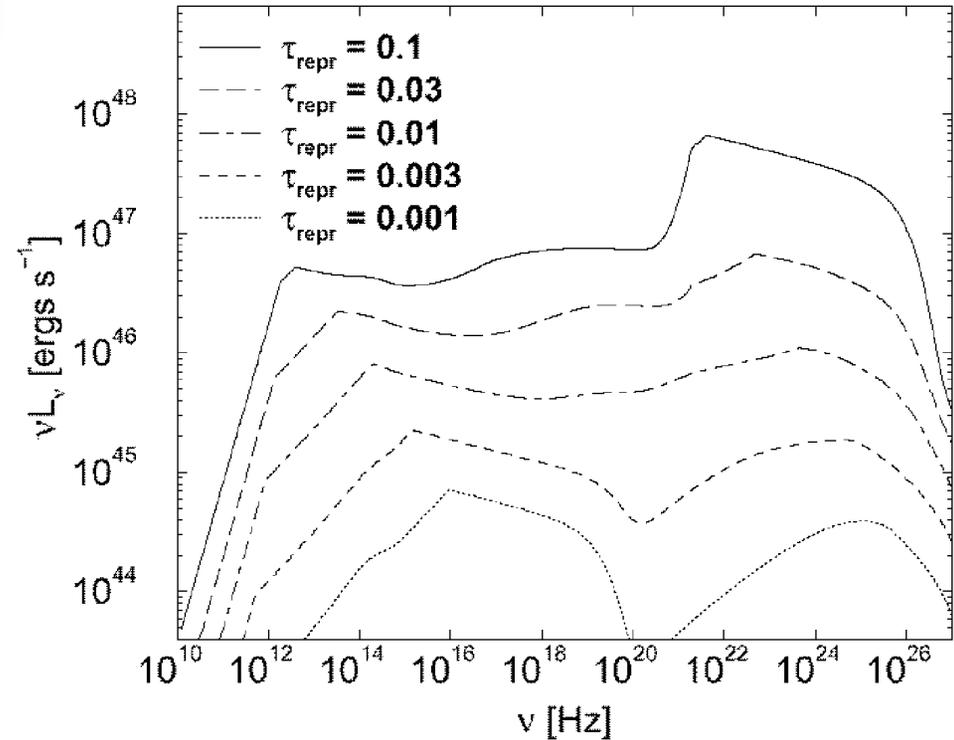
**Simple analytic forms**

# Blazar Main Sequence



Sambruna et al. (1996); Fossati et al. (1998)

Flaring vs. quiescent behavior



Evolution from FSRQ to BL Lac Objects  
in terms of a reduction of fuel from  
surrounding gas and dust

Böttcher and Dermer (2000)  
Cavaliere and d'Elia (2000)

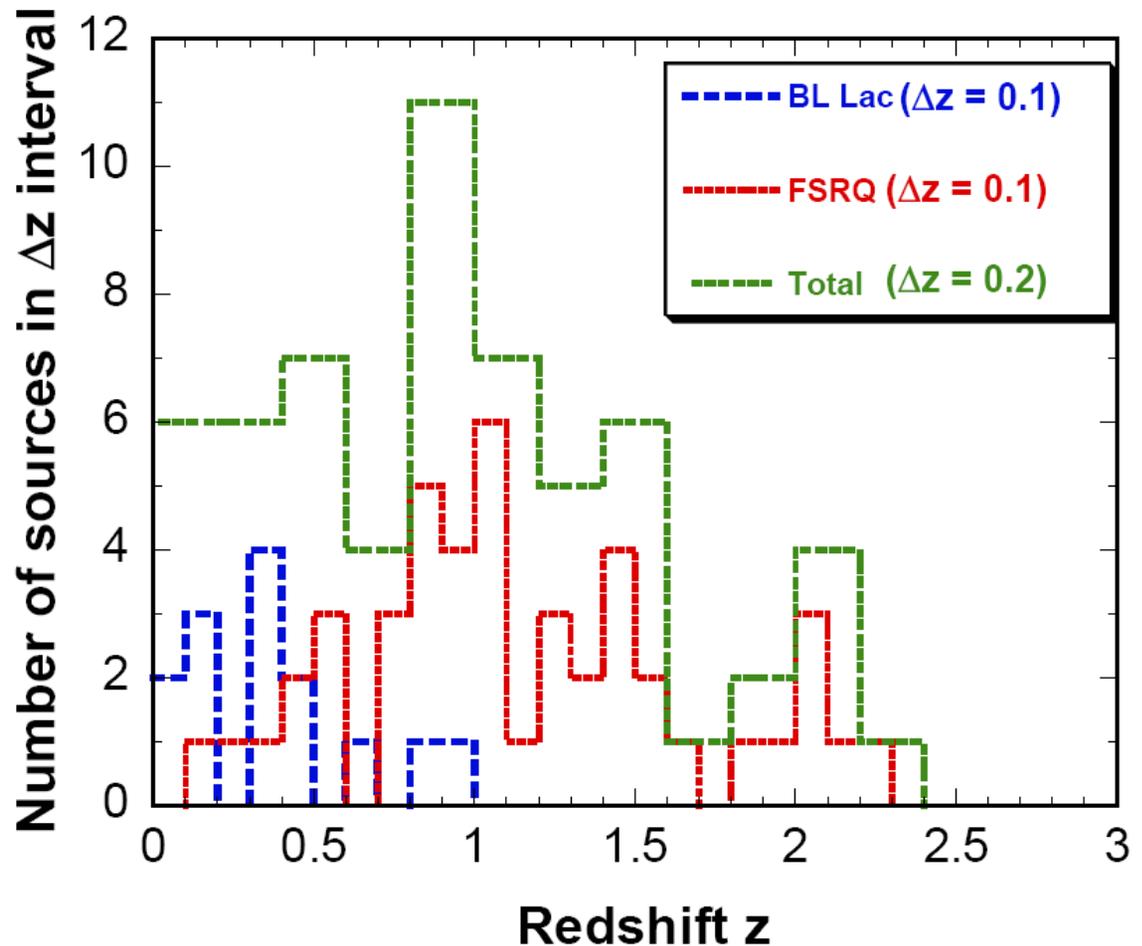
## Observed redshift distribution of blazars

**Redshift distribution of EGRET blazars (histograms), separated into 46 FSRQs and 14 BL Lac Objects (BLs).**

**Uniform exposure: EGRET all-sky survey**

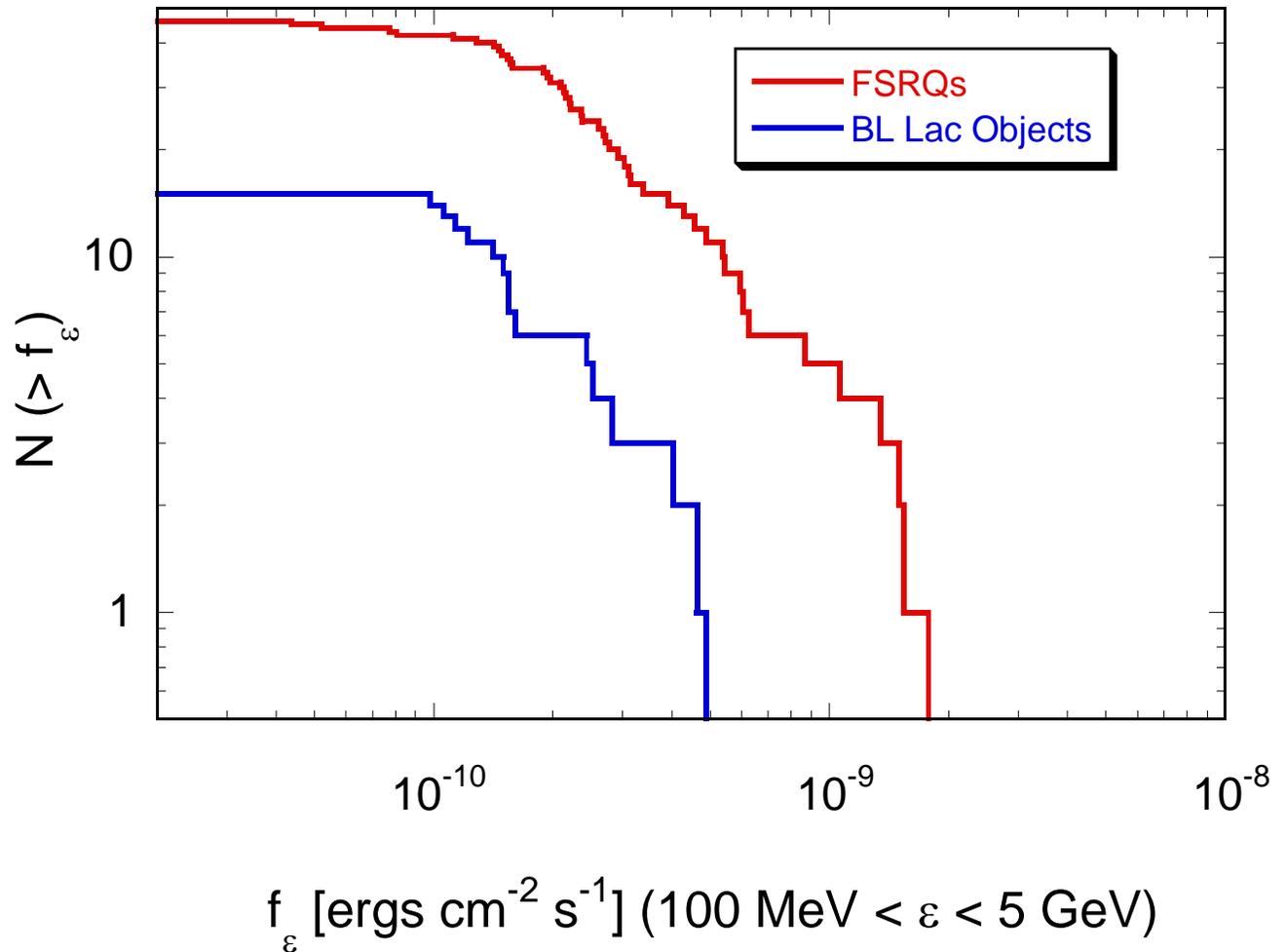
Fichtel et al. (1994):  
1EG

GLAST: essentially uniform exposure



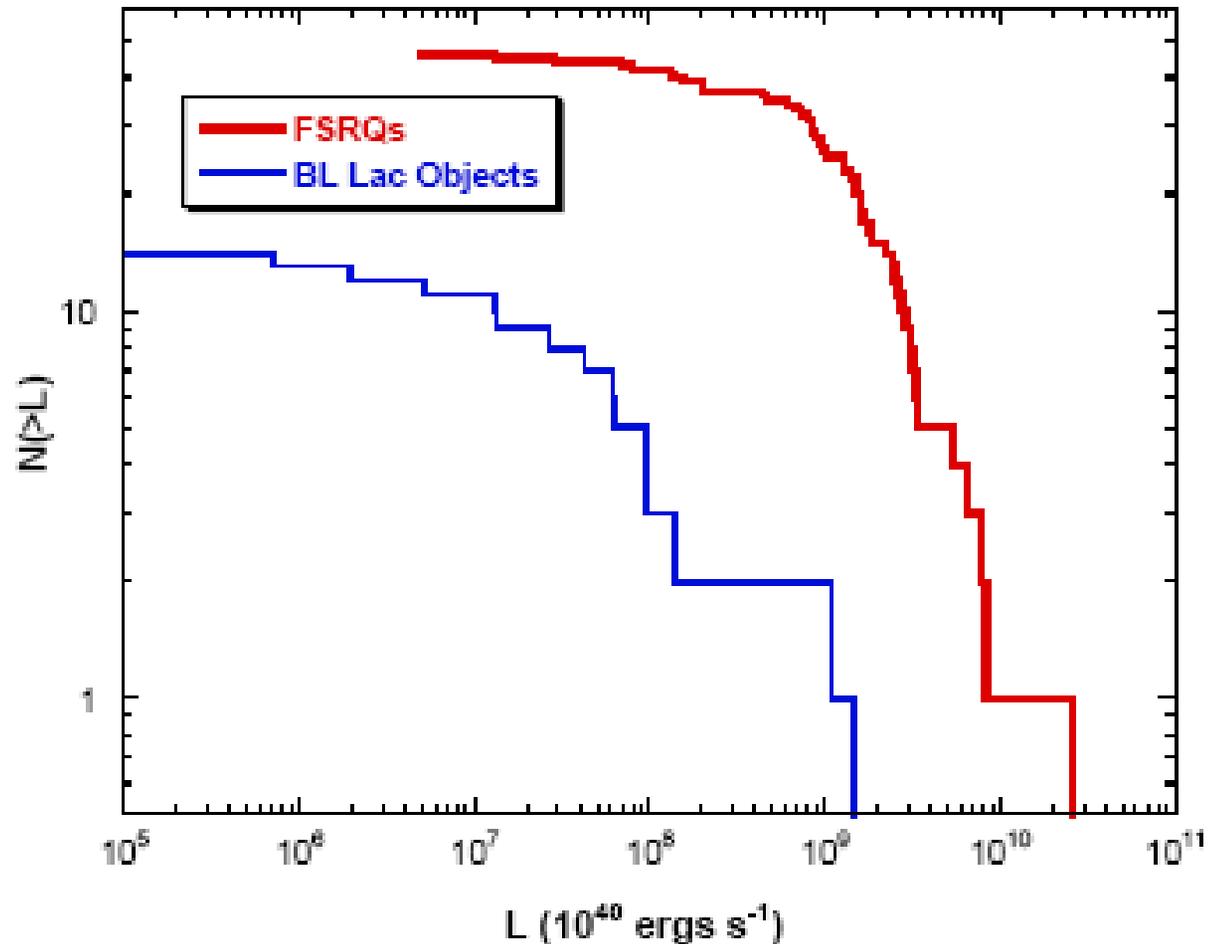
(Peak) flux distribution of EGRET Blazars

Histogram showing the measured peak power flux size distribution of EGRET blazars, separated into FSRQs and BLs



## Measured $\gamma$ -ray blazar peak luminosity distribution

**Distribution of observed peak luminosities of FSRQs and BLs as measured in the EGRET energy range.**



## Statistics of cosmological relativistic jet sources

$\Lambda$ CDM cosmology, bursting sources

$$\frac{d\dot{N}}{d\Omega} = \frac{c}{H_0} \frac{d_L^2 \dot{n}_{co}(L_*, \alpha; z) dL_* d\alpha dz}{(1+z)^3 \sqrt{\Omega_m(1+z)^3 + \Omega_\Lambda}} \quad \hat{f}_{\bar{\epsilon}} : \nu F_\nu \text{ flux threshold}$$

$$\hat{f}_{\bar{\epsilon}} \approx 2 \times 10^{-11} \text{ ergs cm}^{-2} \text{ s}^{-1} : \text{ EGRET} \quad \hat{f}_{\bar{\epsilon}} \approx (1-5) \times 10^{-13} \text{ ergs cm}^{-2} \text{ s}^{-1} : \text{ GLAST}$$

$$\bar{\epsilon} \approx 200 \quad \bar{\epsilon} \approx 200 - 2000$$

Redshift distribution above  $f_\epsilon$

$$\frac{d\dot{N}}{dz d\Omega} (> f_\epsilon) = \frac{c}{H_0} \frac{d_L^2(z) \dot{n}_{co}(z)}{(1+z)^3 \sqrt{\Omega_m(1+z)^3 + \Omega_\Lambda}} [1 - \max(0, \hat{\mu}(z))]$$

Integrate over  $z$  to get  $f_\epsilon$  flare size

distribution:  $p$  for spectrum,  $q$  for beaming factor

$$\hat{\mu}(z) = \frac{1}{\beta} \left\{ 1 - \frac{1}{\Gamma} \left[ \frac{\ell'_e \epsilon_z^{(3-p)/2}}{d_L^2(z) f_\epsilon} \right]^{1/q} \right\}$$

## Redshift distribution of model $\gamma$ -ray blazars: BFH

Histogram showing the model redshift distributions of EGRET blazars, assuming constant comoving density of blazars and an  $\Omega_m = 0.3$ ,  $\Omega_\Lambda = 0.7$  cosmology with a Hubble constant  $H_0 = 72$  for different blazar formation histories (BFHs)

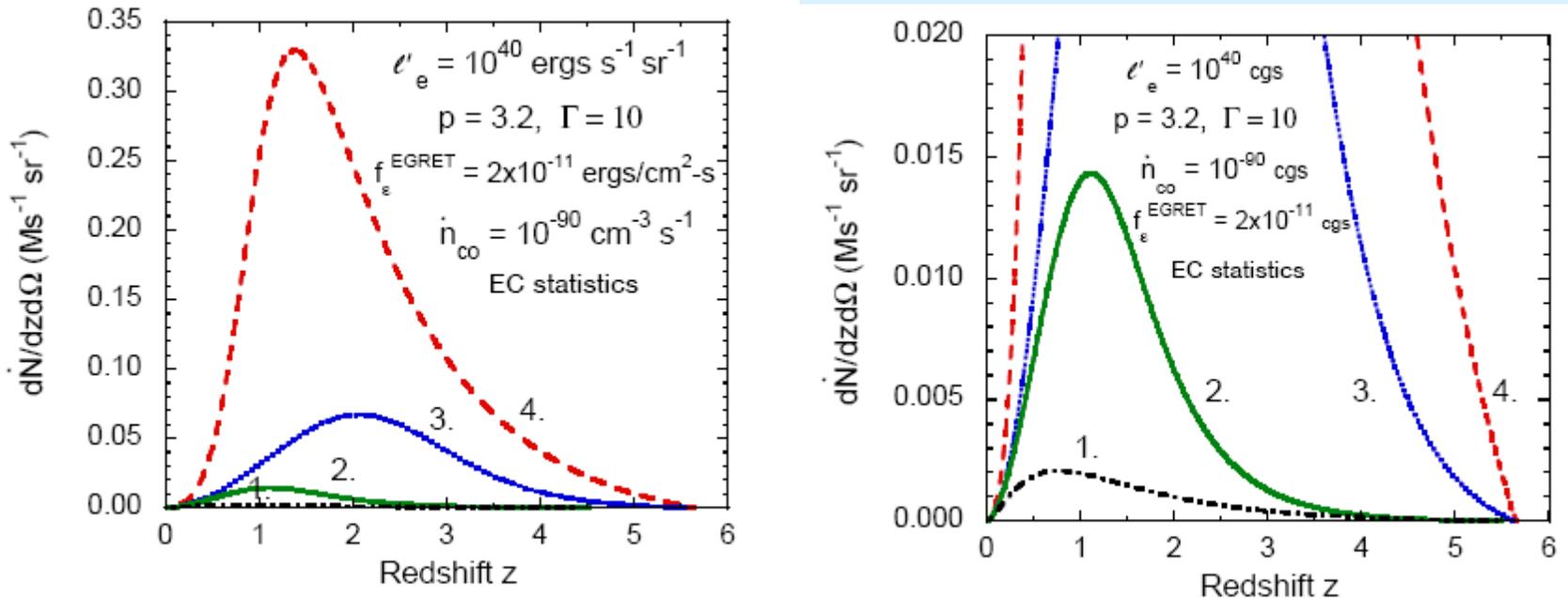


Fig. 4.— Variation in the blazar redshift distribution above an EGRET-type sensitivity threshold  $= 2 \times 10^{-11} \text{ ergs cm}^{-2} \text{ s}^{-1}$  at  $\epsilon \approx 200$  for different blazar formation histories (BLHs). The linear scale on the left shows better BFH3 and 4 (left), and on the right shows better BFH 1 and 2, for standard model blazar with parameters indicated.

# Redshift distribution of model $\gamma$ -ray blazars: $\ell'_e$

Changing comoving directional luminosity.

Standard value is:  $\ell'_e : 10^{40} \text{ ergs s}^{-1} \text{ sr}^{-1}$

Note that BFH3 gives a peak redshift  $\langle z \rangle \sim 2$  rather than  $\langle z \rangle \sim 1$  (observed) unless  $\ell'_e$  or  $\Gamma$  are small

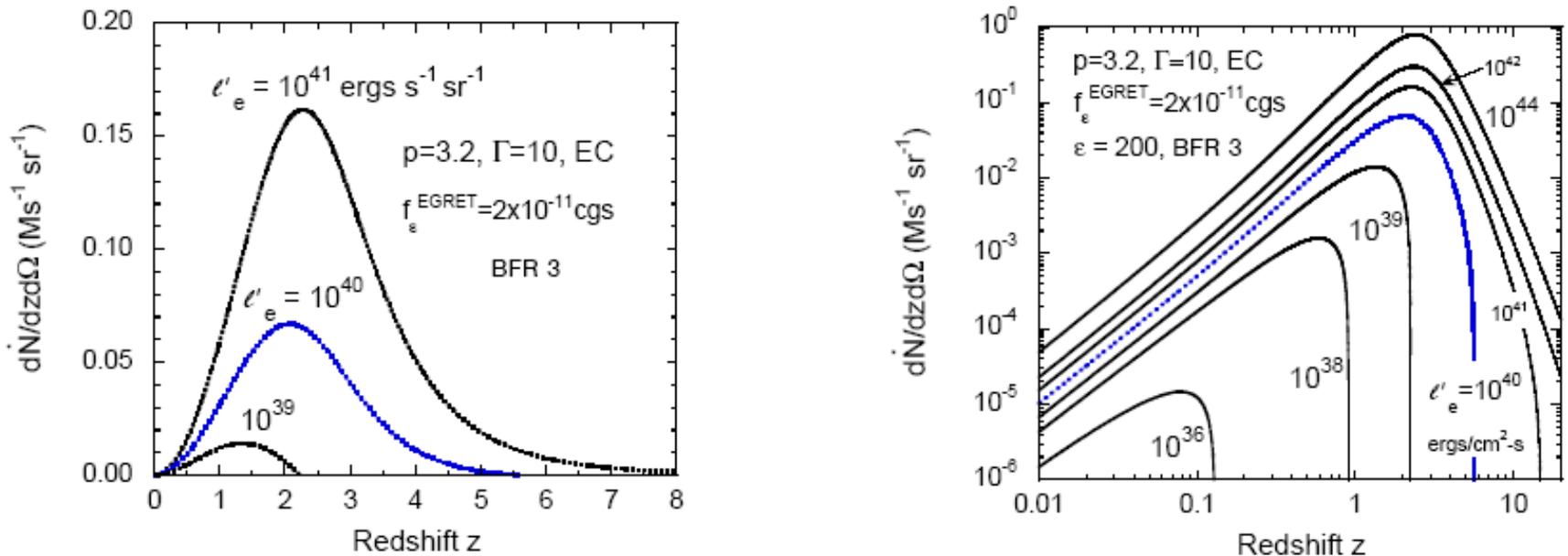


Fig. 5.— Model redshift distributions for standard model blazars with only the comoving power changed, assuming a blazar formation history proportional to the star formation rate history with extinction corrections, BFH 3. (left) On a linear scale, with  $\ell'_e$  changed by only 2 orders of magnitude. (right) On a log-log scale, with  $\ell'_e$  changed by 8 orders of magnitude.

## Redshift distributions of model $\gamma$ -ray blazars: $\Gamma$

Changing  $\Gamma$  factor: standard value is 10; BFR 3

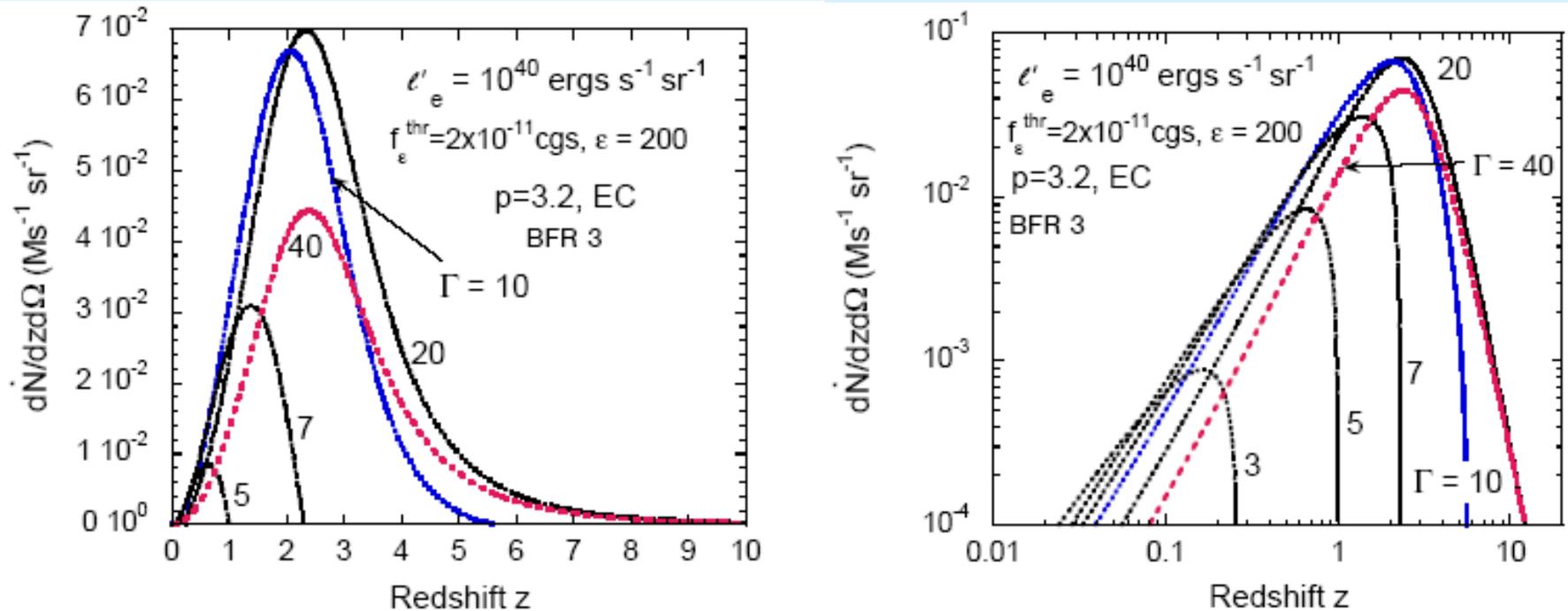


Fig. 6.— Blazar redshift distribution for a model blazar with  $\Gamma$  varied from 3 – 40, for EGRET detection properties, with a  $\nu F_\nu$  threshold sensitivity of  $2 \times 10^{-12} \text{ ergs cm}^{-2} \text{ s}^{-1}$  at  $\epsilon = 200$ . (left) Linear scale. (right) Logarithmic scale.

# Redshift distribution of model $\gamma$ -ray blazars: beaming factor

Note different directional luminosities and  $\Gamma$  factors

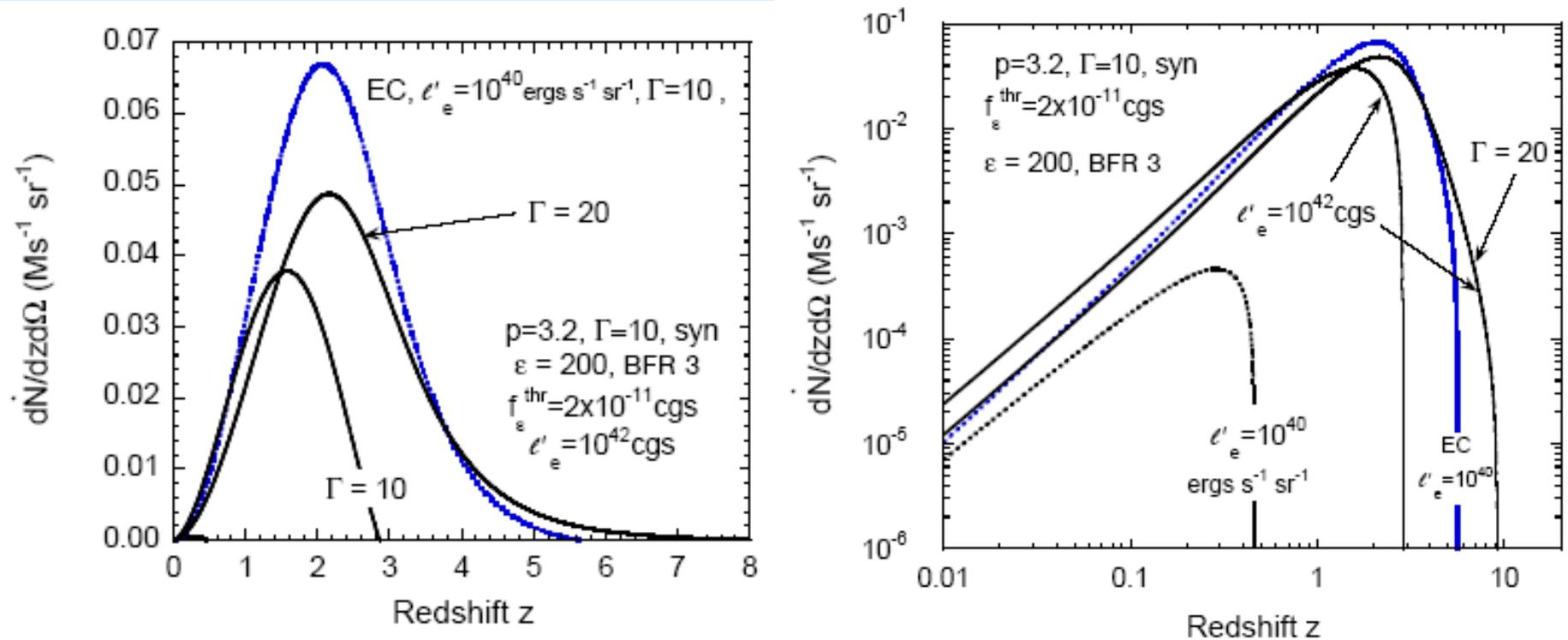


Fig. 7.— Blazar redshift distribution for a model blazar with  $\Gamma = 10$ , EC statistics, and EGRET detection properties (upper blue dotted curve) compared with results for synchrotron statistics, with different directional jet powers  $l'_e$  and  $\Gamma$  factors as labeled. (left) Linear scale. (Right) Logarithmic scale.

## Preliminary predictions for FSRQs

Standard model blazar,  $\Gamma = 10$ , EC, directional luminosity of  $10^{40}$  ergs  $s^{-1}$   $sr^{-1}$ , different BFHs

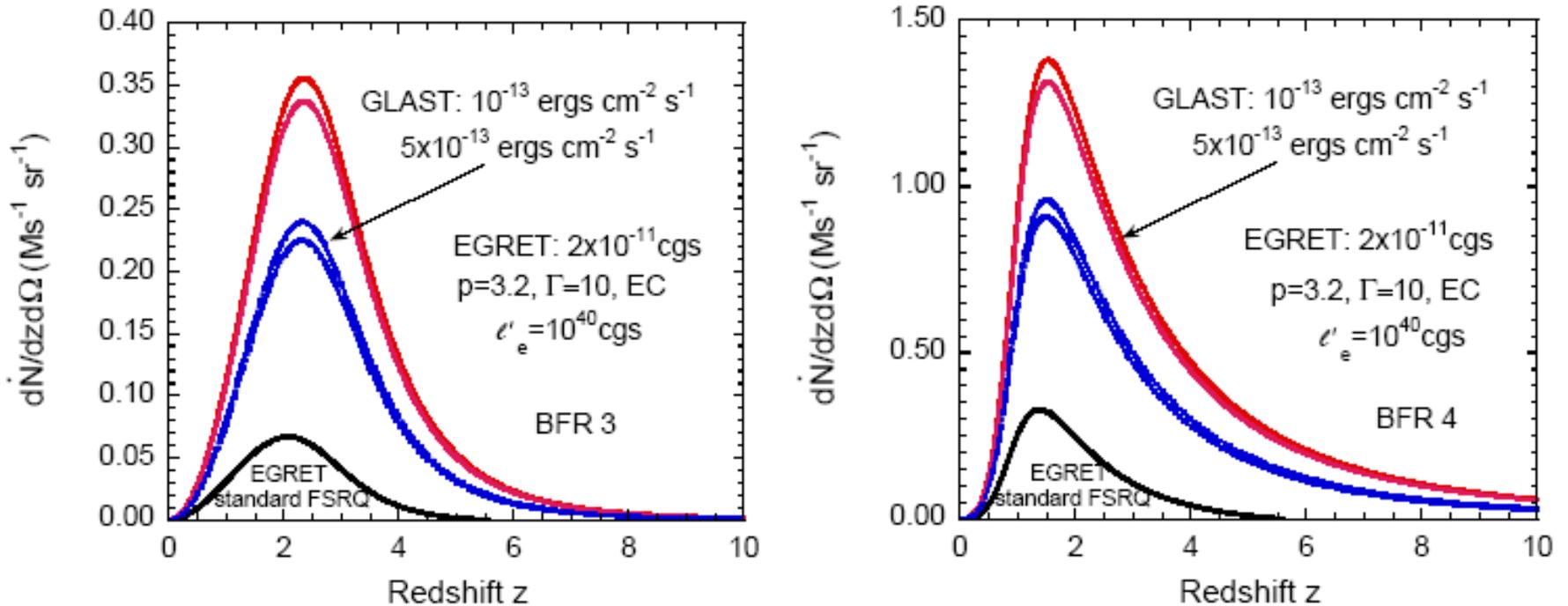
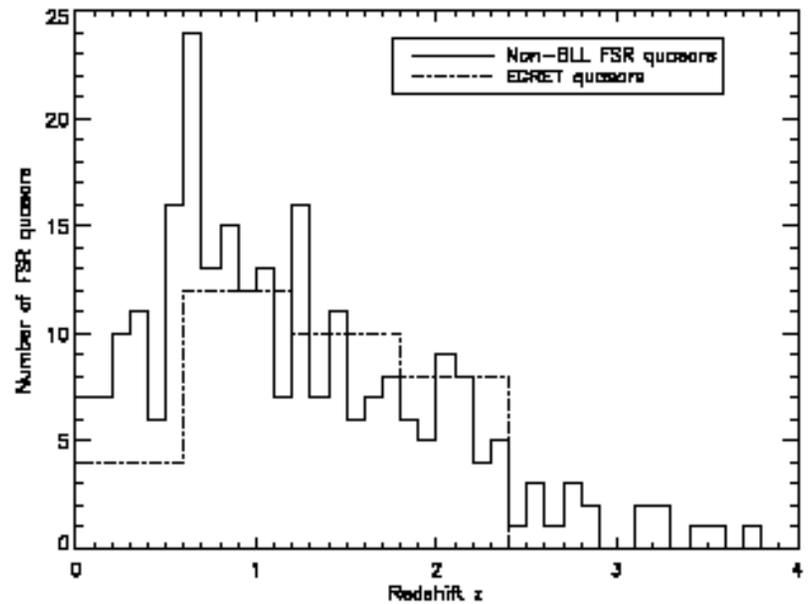
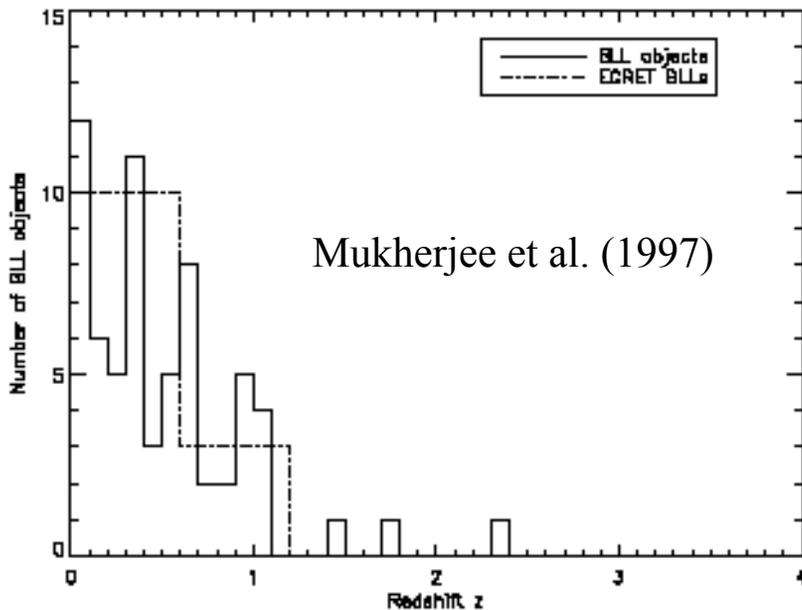


Fig. 8.— Model FSRQ redshift distribution for a standard model blazar with  $\Gamma = 10$ , EC statistics, and EGRET detection properties (upper blue dotted curve), for BFR 3 (left) and BFR 4 (right). GLAST predictions for  $f_e^{thr} = 5 \times 10^{-13}$  ergs  $cm^{-2}$   $s^{-1}$  and for  $f_e^{thr} = 1 \times 10^{-13}$  ergs  $cm^{-2}$   $s^{-1}$  are shown by the middle and upper pairs of curves, respectively. The observing frequency is  $\epsilon = 200$  and  $\epsilon = 2000$  for the higher and lower curve, respectively, in each pair of curves.

**BLs not yet treated**

# GLAST Analysis of Blazars



## Measure three characteristic redshifts:

1. Average redshift  $\langle z \rangle$  for entire sample
2. Average redshift  $\langle z_- \rangle$  for  $z < \langle z \rangle$
3. Average redshift  $\langle z_+ \rangle$  for  $z > \langle z \rangle$

## Determine characteristic redshifts for groupings by:

1. class type (most simply, FSRQ vs. BL)
2. Peak flux or average flux
3. Photon energy

**Better analysis:** Kolmogorov-Smirnov test

## Compare with models:

1. Choose BFR, Statistics
2. Determine best values of  $\Gamma$  and  $l'_e$   
Degeneracy?  
Implications for parent pop?
3. Identify signatures of high-redshift blazars (e.g.,  $\gamma\gamma$  high-frequency dropouts)

# Theoretical Basis for paper by Dermer and Davis (2000)

*NB: Next 3 VGs are historical material, to be redone*

**Fit parameters for the FSRQs are  $\Gamma = 10$  and comoving luminosity  $L = 3 \times 10^{44}$  ergs  $s^{-1}$ ; fit parameters for the BL Lacs are  $\Gamma = 5$  and  $L = 5 \times 10^{44}$  ergs  $s^{-1}$ .**

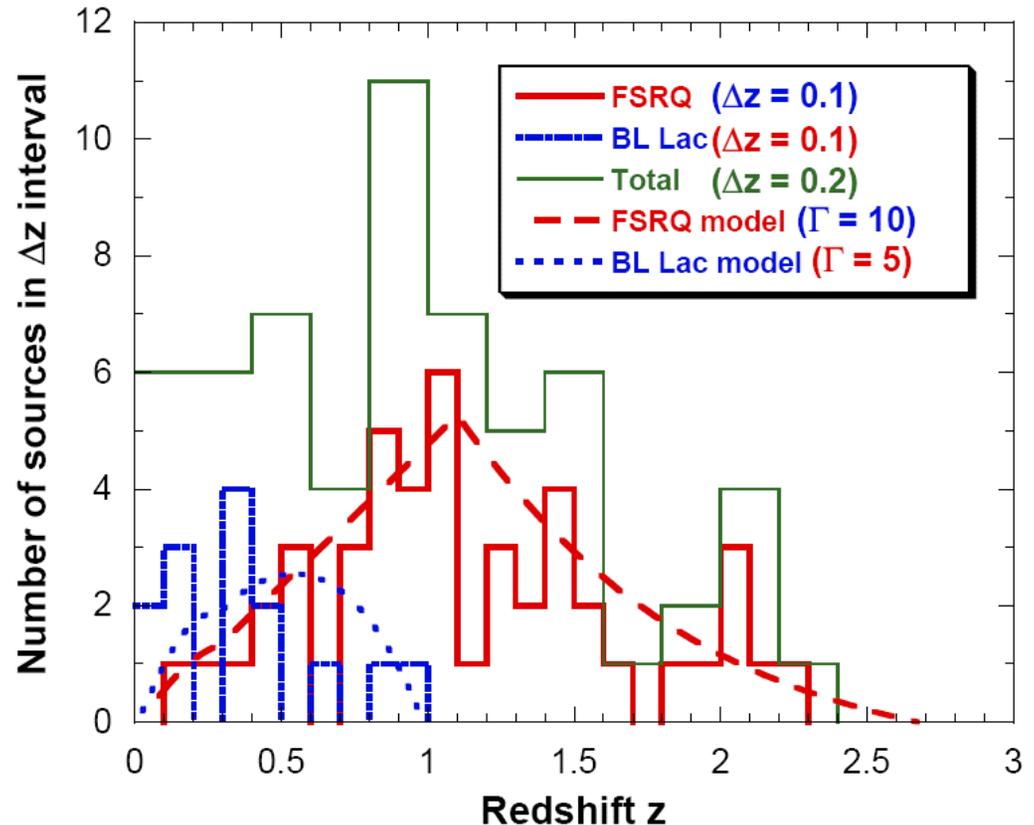
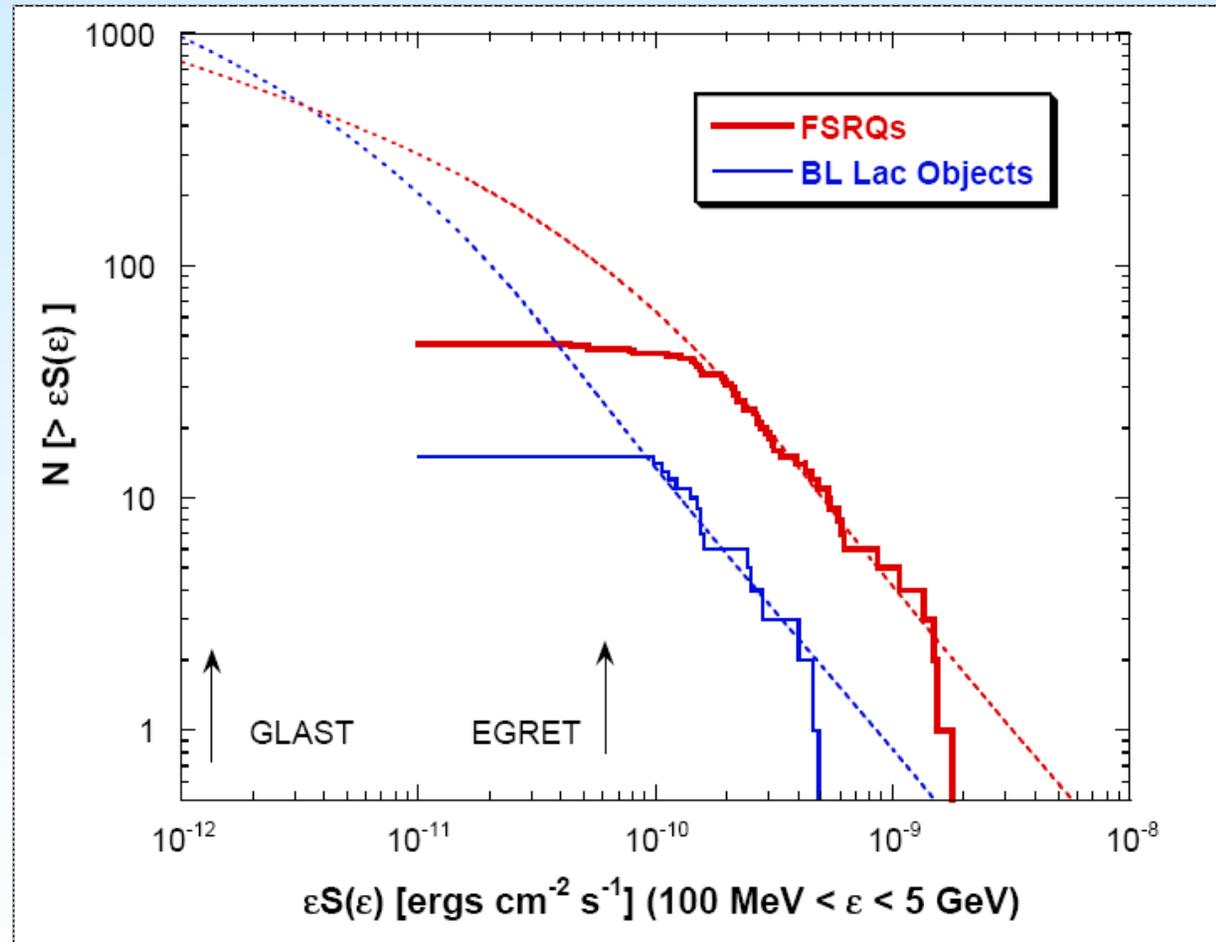


Fig. 1.— Redshift distribution of EGRET blazars (histograms) from the Third EGRET Catalog (3). Curves show model fits assuming comoving density proportional to the star formation rate (SFR; see Fig. 3b). Fit parameters for the FSRQs are  $\Gamma = 10$  and comoving luminosity  $L = 3 \times 10^{44}$  ergs  $s^{-1}$ ; fit parameters for the BL Lacs are  $\Gamma = 5$  and  $L = 5 \times 10^{44}$  ergs  $s^{-1}$ .

## (Peak) flux function of EGRET Blazars

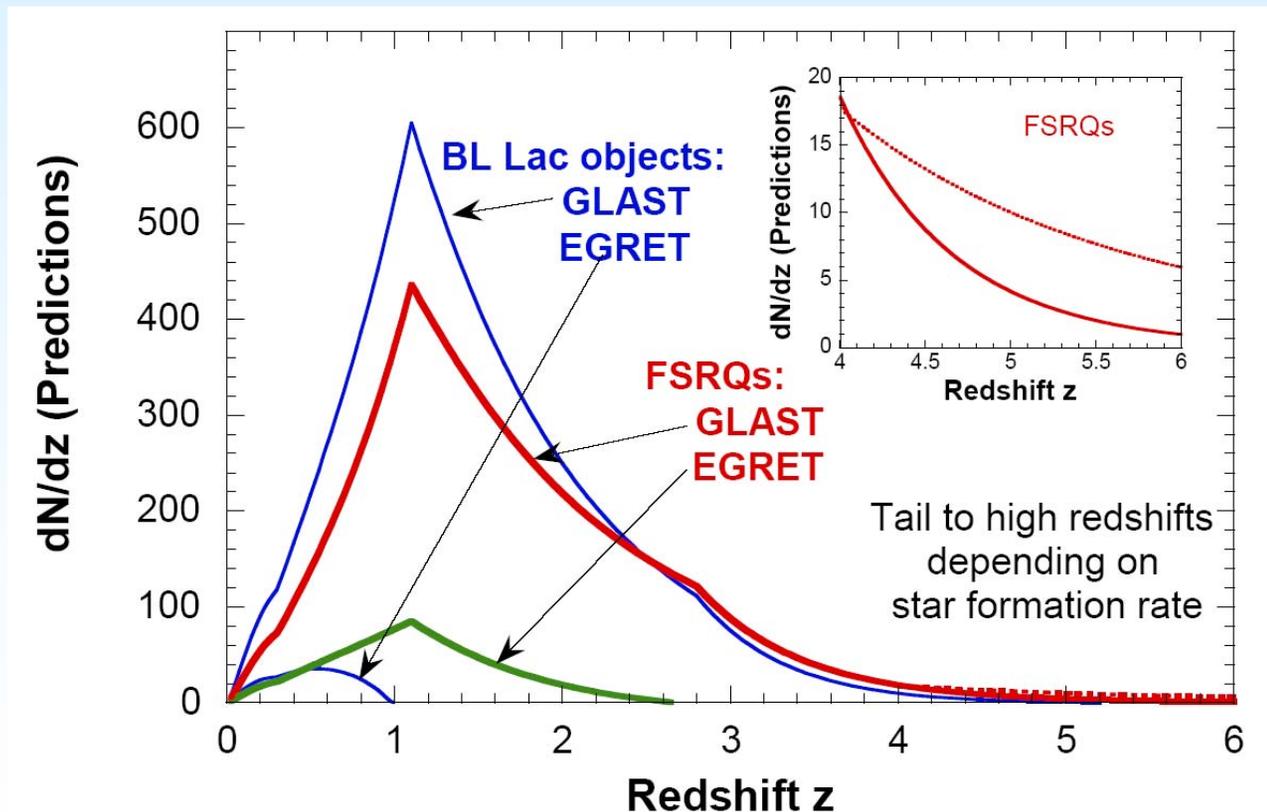
Histogram showing the measured peak power flux size distribution of EGRET blazars, the fit to the size distribution with the model, and predictions for gamma-ray blazar detectability with GLAST for a sensitivity threshold of  $1.3 \times 10^{-12}$  ergs  $\text{cm}^{-2}$   $\text{s}^{-1}$



*NB: GLAST is much more sensitive than this: but this preserves a ratio of 50:1 (GLAST vs. EGRET)*

## Predictions for GLAST

Predictions for the number of FSRQs and BLs to be detected with GLAST, assuming that the blazar rate follows the SFR history of the universe. Inset shows the range of high-redshift blazars implied by uncertainties in the SFR at large redshift



# Diffuse $\gamma$ -Ray Background

$$\epsilon I_\epsilon = \frac{c}{4\pi H_0} \int_0^\infty dz \int d\Omega_* \frac{\epsilon_*^2 q_{co}(\epsilon_*, \Omega_*; z)}{(1+z)^3 \sqrt{\Omega_m(1+z)^3 + \Omega_\Lambda}}$$

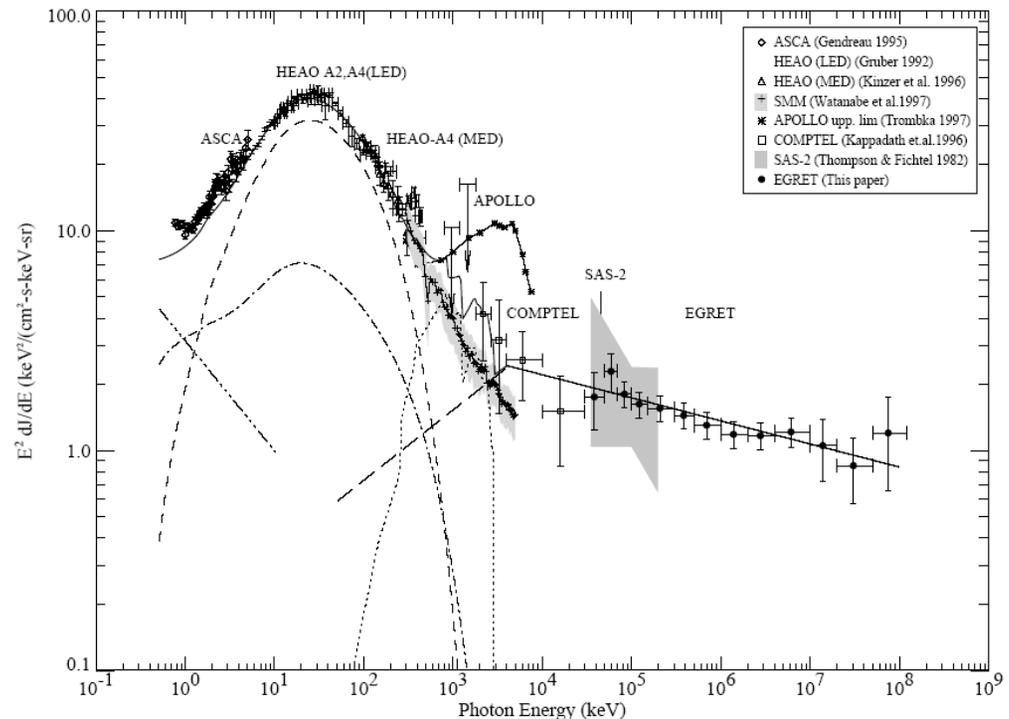
$$q_{co}(\epsilon_*, \Omega_*; z) = \frac{dN_\gamma}{d\epsilon_* dt_* dV_* d\Omega_*}$$

$$\epsilon_*^2 q_{co}(\epsilon_*, \Omega_*; z) = n_{co}(z) \epsilon_* J^s(\epsilon_*)$$

Subtract known point sources

Divide blazar class into  
persistent plus flaring  
component

Sreekumar et al. (1998)



# Redshift evolution of $\gamma$ -ray blazars

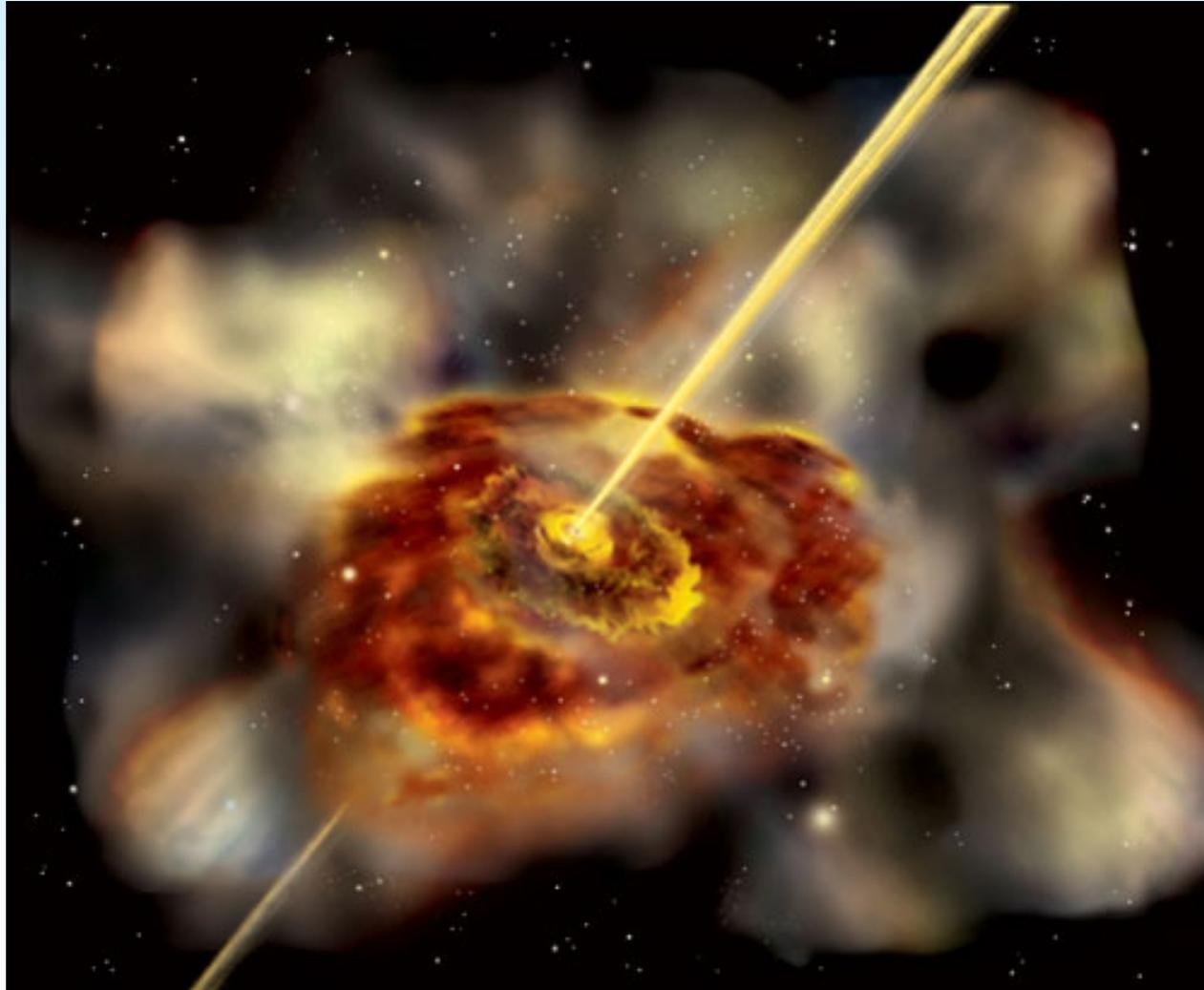
## Black Hole Activity through cosmic time

Relax assumption that

$$\Gamma(z) = \Gamma$$

$$l'_e(z) = l'_e$$

**Feasible with GLAST observations**



## *Summary: What we need from and for GLAST*

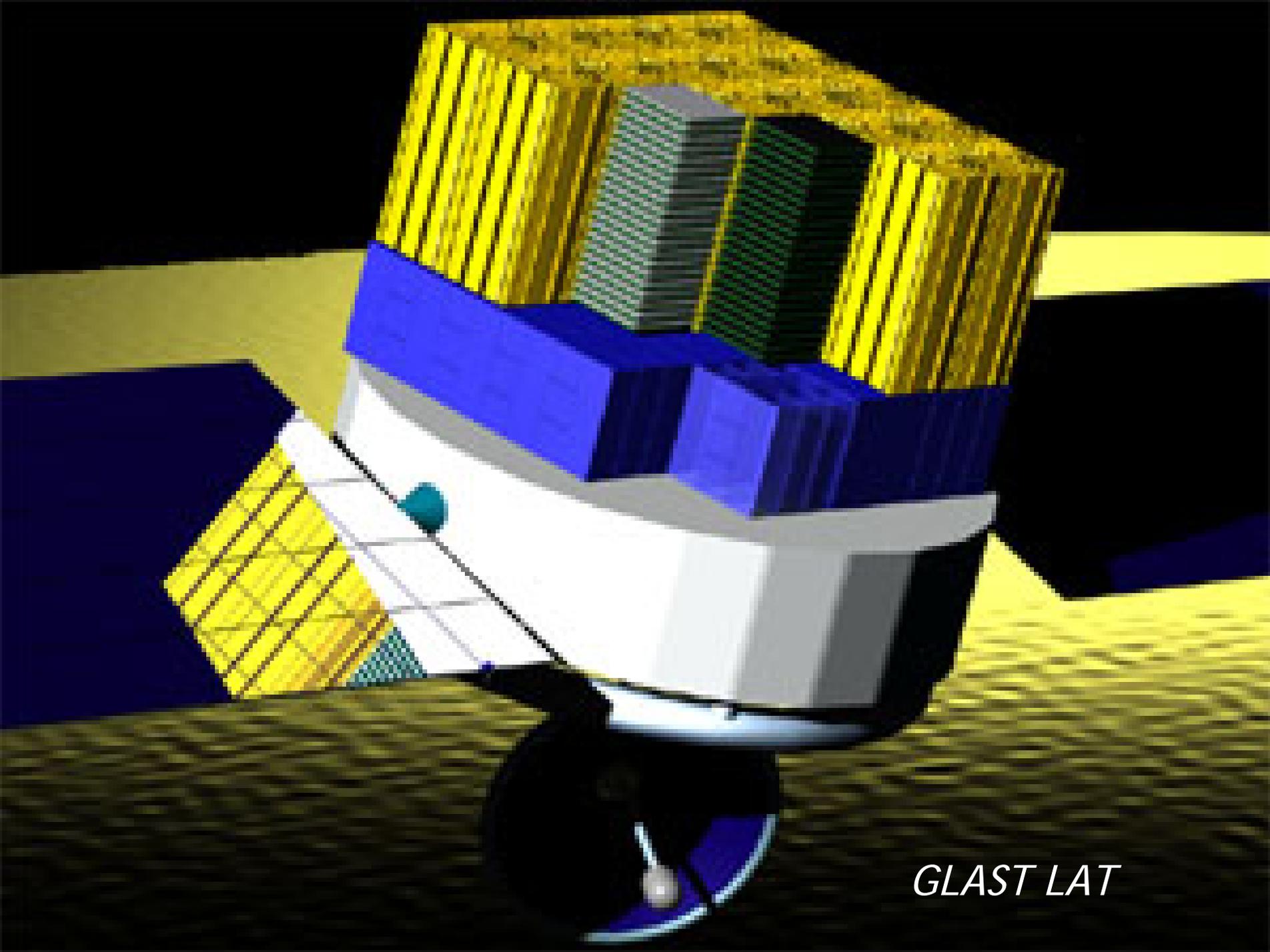
- **Blazar catalogs and identification** (Romani et al.)
  - a. Divide blazars into radio galaxies, BL Lac objects, LBL, and FSRQ (more or less BL Lac-like and FSRQ-like)
  - b. Divide blazar class into persistent plus flaring component
  - c. Host galaxies of blazars: cosmic evolution
- **Redshift distribution for different source classes, different peak-flux ranges:**  
Minimal analysis: calculate 3 characteristic redshifts, compare with models  
Better analysis: KS comparison
- **Peak flux size distribution for different source classes, different redshift ranges**
- **Prediction: GLAST will see a larger ratio of BL Lacs/FSRQs than EGRET**

**Cosmic evolution of supermassive black holes** (tracks IR rather than SFR?)

**Highly-evolved structure formation in early universe**

**Highest redshift persistent and persistently flaring sources**

**EBL**



*GLAST LAT*